

Machine Learning

Instructors: Lei Li, **Yu-Xiang Wang**

About myself

Yu-Xiang Wang 王宇翔

Eugene Aas Chair Assistant Professor

Department of Computer Science,
and Department of Statistics (By Courtesy)

Co-Director, [Center for Responsible Machine Learning](#)

UC Santa Barbara

Office: Henley Hall 2013

E-mail: yuxiangw AT cs.ucsb.edu

Curriculum Vita: [\[link\]](#)

Yu-Xiang is pronounced approximately as ['ju:'ʃi:ɒŋ],
namely, y~eu~ee - sh~ih~ah~ng .

Research area: Statistical Machine Learning. Optimization, reinforcement learning, differential privacy, deep learning.

Short biography:

China => Singapore

⇒ PhD from Carnegie Mellon University

⇒ Scientist at Amazon AI

⇒ Professor at UCSB

Homepage:

<https://cs.ucsb.edu/~yuxiangw/>

Professor Lei Li



Lei Li

Assistant Professor

Computer Science Department
University of California Santa Barbara

Research area: natural language processing, machine learning, data mining.

Topics:

- Machine translation, speech translation, multilingual NLP.
- Text generation and summarization.
- Reasoning and question answering.
- Information extraction.
- AI for drug discovery
- Green and Efficient ML
- Time series mining and prediction
- Probabilistic inference, Bayesian sampling methods

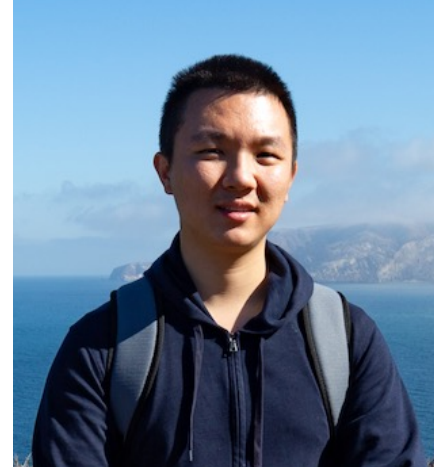
Looking for highly motivated students to join my lab.

UCSB students: please feel free to contact me if you would like to do intern in my lab.

Website: <https://sites.cs.ucsb.edu/~lilei/>

Teaching Assistant

- TA: Xuandong Zhao
- PhD student in CS
- Research focus:
 - Machine Learning
 - Natural Language Processing
 - Privacy and confidentiality

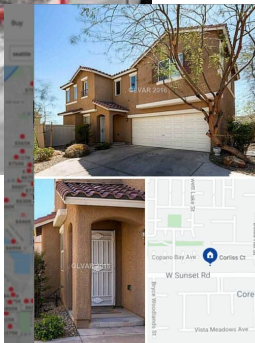


Welcome to CS291K Machine Learning!

- This is a graduate-level **introduction** to machine learning.
 - It gives a comprehensive treatment to ML
 - It covers the theory, algorithms and practical implementation of ML all in 12 weeks!
- This will be a tough course
 - Nevertheless, it's a course worth spending time on.
 - Especially if you are just starting your PhD studies.
- UCSB Covid policy: <https://www.ucsb.edu/COVID-19-information/campus-updates>
 - it's your choice on mask-wearing, but highly recommended to keep everybody in the class.

[Discussion] Why are you taking this course?

~~AI~~ Machine Learning has revolutionized almost every aspect of our daily life



Zillow Edit Save Share More Close

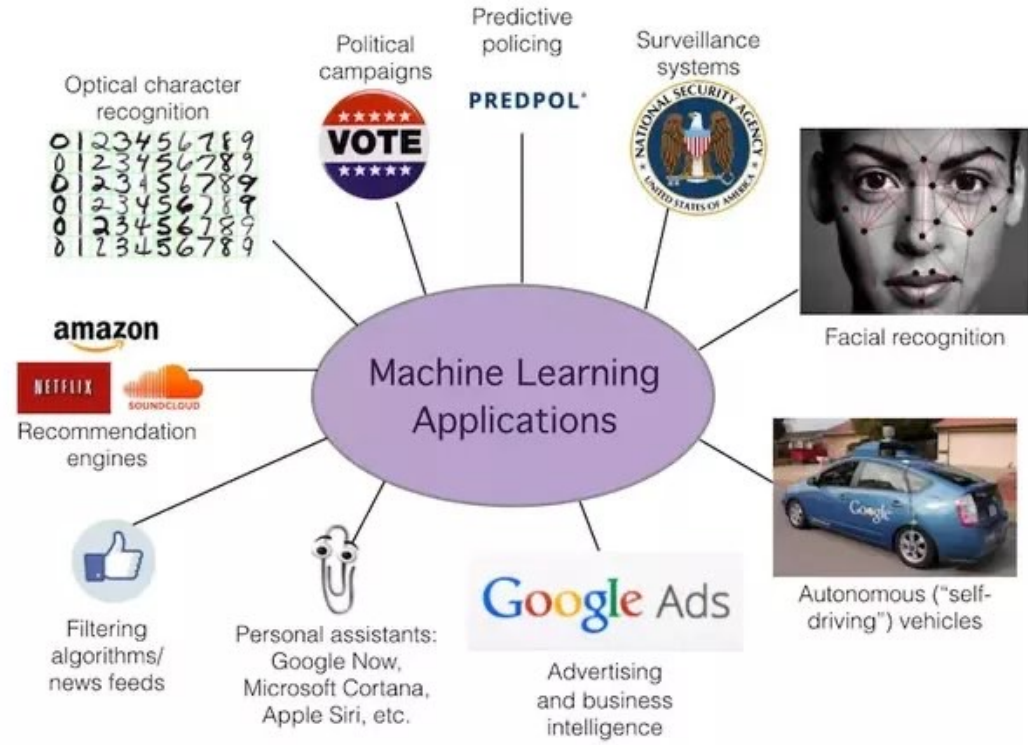
3 bd | 3 ba | 1,417 sqft
123 Main Street, Las Vegas, NV 89148
Off market | Zestimate®: \$266,436 | Rent Zestimate®: \$1,525/mo
Est. refi payment: \$1,277/mo See current rates

Home value Comparable homes Ways to sell Owner tools

Sell to Zillow for your Zestimate
Qualifying homes get a competitive cash offer.

\$266,500
Before taxes & fees

Get your offer



Machine Learning Kaggle

Credit Card Risk Assessment



RISK



Breakthroughs with deep learning

The screenshot shows a web browser displaying a news article on the TechNewsWorld website. The browser's address bar shows the URL www.technewsworld.com/story/84013.html. The page header includes the site name 'TECHNEWSWORLD' and the section 'EMERGING TECH'. A search bar is located in the top right. Below the header, there are navigation links for 'Computing', 'Internet', 'IT', 'Mobile Tech', 'Reviews', 'Security', 'Technology', and 'Tech Blog', along with 'Reader Services'. The main article title is 'Microsoft AI Beats Humans at Speech Recognition' by Richard Adhikari, dated Oct 20, 2016. The article features a central image of a hand pointing at a hexagonal grid with 'AI' in the center, surrounded by terms like 'Artificial Intelligence', 'Reasoning', 'Computer', 'Knowledge', 'Learning', 'Science', and 'Technology'. To the left of the image are social sharing buttons for Google+, Twitter (25), Facebook (45), LinkedIn (11), and a generic share button (104). To the right of the image are 'Print' and 'Email' options. Below the image is the first paragraph of the article, which states that Microsoft's AI unit reported surpassing human transcriptionists. On the right side of the page, there are social media icons for Facebook, Twitter, LinkedIn, Google+, SoundCloud, and RSS. Below these are links for 'Most Popular', 'Newsletters', and 'News Alerts'. A poll titled 'How do you feel about Black Friday and Cyber Monday?' is visible, with five radio button options and a 'Vote to See Results' button. Below the poll is an 'E-Commerce Times' section with several headlines: 'Black Friday Shoppers Hungry for New Experiences, New Tech', 'Pay TV's Newest Innovation: Giving Users Control', 'Apple Celebrates Itself in \$300 Coffee Table Tome', 'AWS Enjoys Top Perch in IaaS, PaaS Markets', and 'US Comptroller Gears Up for Blockchain and...'. The page footer shows the number '8'.

www.technewsworld.com/story/84013.html

TECHNEWSWORLD EMERGING TECH

Computing Internet IT Mobile Tech Reviews Security Technology Tech Blog Reader Services

Microsoft AI Beats Humans at Speech Recognition

By Richard Adhikari
Oct 20, 2016 11:40 AM PT

Print Email

Artificial Intelligence
Reasoning
Computer
Knowledge
Learning
Science
Technology
System

AI

Image: Adobe Stock

Microsoft's Artificial Intelligence and Research Unit earlier this week reported that its speech recognition technology had surpassed the performance of human transcriptionists.

How do you feel about Black Friday and Cyber Monday?

- They're great -- I get a lot of bargains!
- The deals are too spread out -- I'd prefer just one day.
- They're a fun way to kick off the holiday season.
- I don't like the commercialization of Thanksgiving Day.
- They're crucial for the retail industry and the economy.
- The deals typically aren't that good.

Vote to See Results

E-Commerce Times

- Black Friday Shoppers Hungry for New Experiences, New Tech
- Pay TV's Newest Innovation: Giving Users Control
- Apple Celebrates Itself in \$300 Coffee Table Tome
- AWS Enjoys Top Perch in IaaS, PaaS Markets
- US Comptroller Gears Up for Blockchain and...

Breakthroughs with deep learning

The image shows a screenshot of a web browser displaying a Google blog post. The browser's address bar shows the URL: <https://blog.google/products/translate/round-translation-more-accurate-fluent-sentences-google-translate/>. The browser's bookmark bar contains several items, including '40 maps that explain', 'Amazon Web Services', 'Primers | Math n Proc', 'deeplearning.net/tut...', 'Deep Learning Tutori...', 'deep learning', 'PHILIPS - Golden Ears', 'Language Technologi...', 'MyIDCare - Dashboar...', and 'Other bookmarks'. The blog post itself has a yellow header with the word 'TRANSLATE' on the left and the date 'NOV 15, 2016' on the right. The main title of the post is 'Found in translation: More accurate, fluent sentences in Google Translate'. Below the title, the author is identified as 'Barak Turovsky' with the role 'PRODUCT LEAD, GOOGLE TRANSLATE'. At the bottom of the visible content, there is a snippet of text: 'In 10 years, Google Translate has gone from supporting just a few languages to 103, connecting strangers, reaching across language barriers and even helping'. A blue circular share icon is visible in the bottom right corner of the page content.

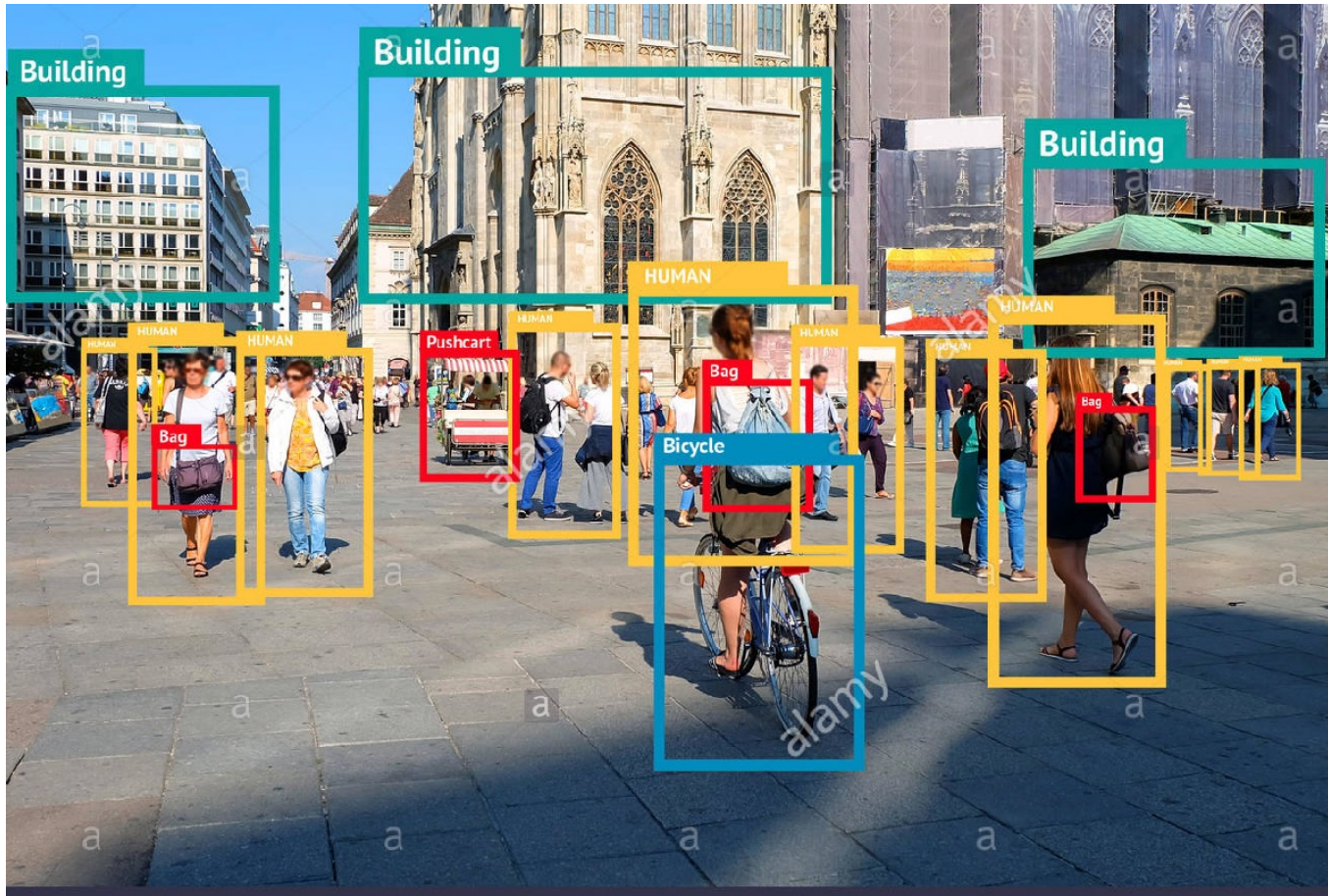
TRANSLATE NOV 15, 2016

Found in translation: More accurate, fluent sentences in Google Translate

Barak Turovsky
PRODUCT LEAD, GOOGLE TRANSLATE

In 10 years, Google Translate has gone from supporting just a few languages to 103, connecting strangers, reaching across language barriers and even helping

Image segmentation and object recognition



Achieving Master Level in GO

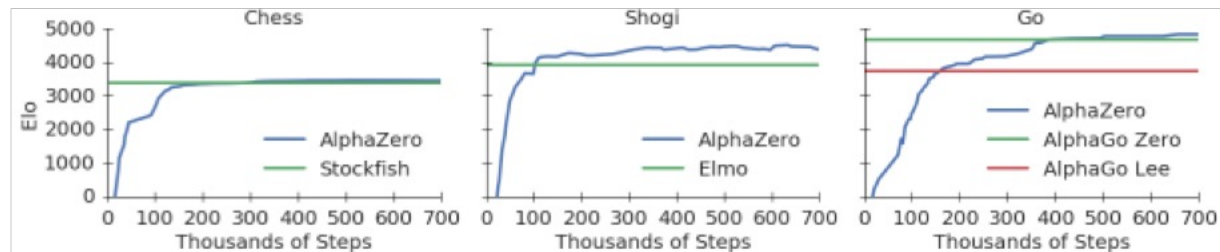
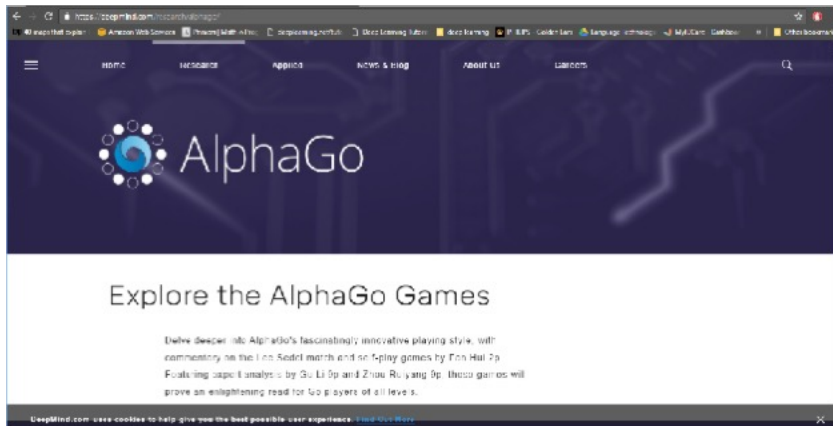


Figure 1: Training *AlphaZero* for 700,000 steps. Elo ratings were computed from evaluation games between different players when given one second per move. **a** Performance of *AlphaZero* in chess, compared to 2016 TCEC world-champion program *Stockfish*. **b** Performance of *AlphaZero* in shogi, compared to 2017 CSA world-champion program *Elmo*. **c** Performance of *AlphaZero* in Go, compared to *AlphaGo Lee* and *AlphaGo Zero* (20 block / 3 day) (29).

Image Captioning

Human captions from the training set



A cute little **dog** **sitting** in a heart drawn on a sandy **beach**.



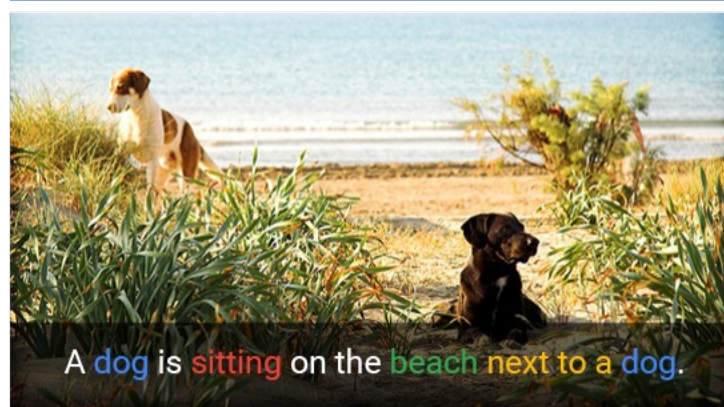
A **dog** walking **next to** a little **dog** on top of a **beach**.



A large brown **dog** **next to** a small **dog** looking out a window.



Automatically captioned

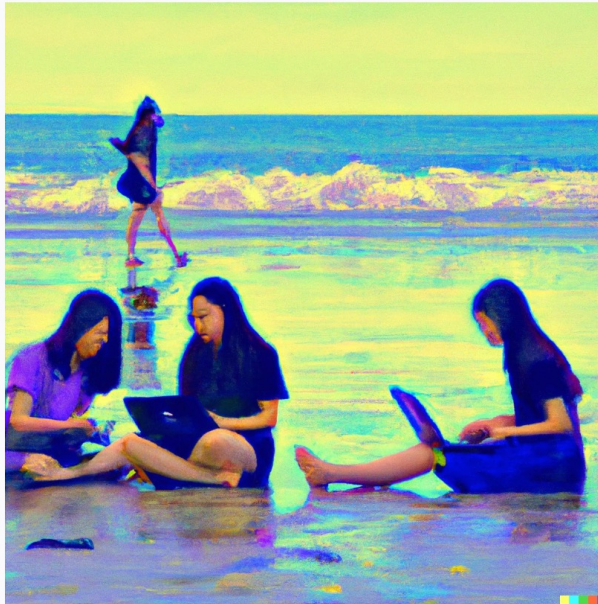
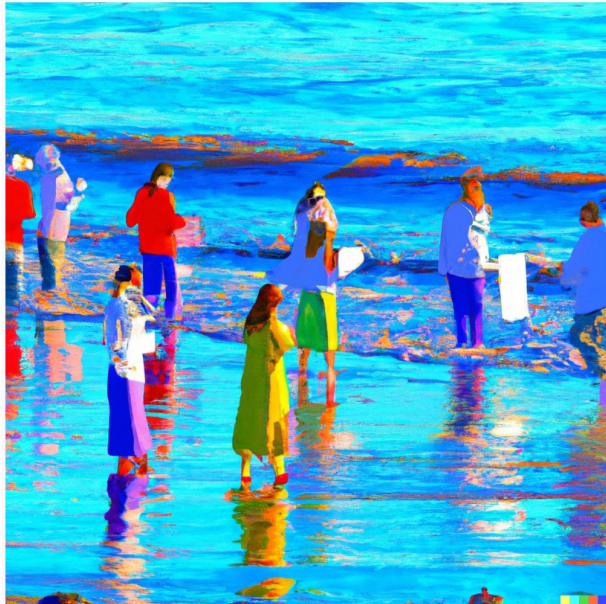


A **dog** is **sitting** on the **beach** **next to** a **dog**.

Art generation

Tell DALL E 2:

“Students eager to learn machine learning on a Californian beach in Monet style”



ML Is Transforming The Industries

- ML has transformed the IT industry
 - Search Engine
 - Speech Recognition
 - Machine Translation
 - Recommendation
- ML is transforming other industries
 - Transportation
 - Healthcare
 - Finance
 - Insurance, Law, HR, Travel, Media, ...
 - Semiconductor / Microprocessors

ML is transforming the academia

- SOTA methods in computer vision / speech recognition / natural language processing
- Recent candidates who interviewed with UCSB for faculty positions
 - Top security person: doing security + ML
 - Top database person: doing ML for databases
 - Top software engineering person: doing software engineering for ML systems debugging.
 - Of course, we also interviewed quite a few core ML/ AI candidates too

Why should you learn ML?

- Career opportunities
 - AI / ML jobs are highly paid
 - AI / ML are becoming the standard tools all software engineers are expected to know.
- Research opportunities and potential impact
 - “The golden age of physics is Newton’s time and Einstein’s time, the golden age of AI is right now!”
- Personal development
 - Consolidate your knowledge, connect the dots
 - Becoming better in solving problems
- “It is just my passion! ”

How can this course help you?

- At the end of the course you will be able to
 1. Understand jargons of ML
 2. Assess whether ML will be a good solution to your problem; if so, choose appropriate ML models for it
 3. Correctly implement and debug each step of ML workflow
 4. Develop theoretical understanding on how / why / when ML works.
 5. Read research papers in ML (possibly ready to write your own)

Topics we will cover

| # | Date | Topic | |
|----|-------|--|-----------------------------|
| 1 | 9/22 | Introduction, Supervised Learning, Linear regression | Machine Learning basics |
| 2 | 9/27 | Classification, Linear Classifier, Decision Tree | |
| 3 | 9/29 | Unsupervised Learning, dimensionality reduction | |
| 4 | 10/4 | Optimization basic: Gradient Descent and SGD | |
| 5 | 10/6 | Feedforward Neural Networks | Modern Deep Learning models |
| 6 | 10/11 | Convolutional Neural Networks | |
| 7 | 10/13 | Sequence Modeling and Recurrent Neural Networks | |
| 8 | 10/18 | Attention Mechanism and Transformers | |
| 9 | 10/20 | Graphical Models and MLE | Probabilistic ML models |
| 10 | 10/25 | Gaussian Mixture Models, EM, LDS | |
| 11 | 10/27 | Undirected Graphical Models, Conditional Random Fields | |
| 12 | 11/1 | Deep Latent Model and Approximate Inference | |
| 13 | 11/3 | Sampling Methods | Optimization-based methods |
| 14 | 11/8 | Convex Optimization | |
| 15 | 11/10 | Support Vector Machine, Kernel Methods | |
| 16 | 11/15 | Online Learning | ML Foundations |
| 17 | 11/17 | Statistical Learning Theory I | |
| 18 | 11/22 | Statistical Learning Theory II | |
| 19 | 11/29 | Theory of Deep Learning and Overparameterization | |
| 20 | 12/1 | Reinforcement Learning | |
| | | Final project poster presentation | |

Course information

- Websites

- <https://sites.cs.ucsb.edu/~lilei/course/ml22fa/index.html>
- Schedule, lecture notes, assignments, related links

- Discussion on Ed:

- <https://edstem.org/us/courses/22801/discussion/>

- Reference books

- [PRML] Pattern Recognition and Machine Learning, Bishop. available [online](#)
- [FML] Foundations of Machine Learning. Mohri, Rostamizadeh, and Talwalkar. available [online](#).
- [D2L] Dive into Deep Learning. Zhang, Lipton, Li, Smola. available [online](#).
- [MML] Mathematics for Machine Learning, Deisenroth, Faisal, and Ong. Free [online](#).

Workload and grades

- 50% Homework assignments
 - HW0: 5%
 - HW1-3: 15% each
 - A mix of theory questions and coding questions
 - Each student needs to write their own homework (discussion / collaboration allowed if declared)
- 40% Project
 - Proposal 5%
 - Midterm milestone 5%
 - Presentation 10% + Final report 20%
- 10% In-class or short after-class quiz
 - You only need to complete them to get the credits

Project timeline

- Group size: 1 – 4
- Milestones:
 - Proposal due 10/6: one pager on what you will do
 - Midterm milestone 11/3: one pager update
 - Poster presentation: early December
 - Final report: Shortly after the presentation
- Basic project:
 - Read a paper, replicate results
- Advanced project:
 - Apply ML to your problem / data from your research
 - Develop new ML methods / theory

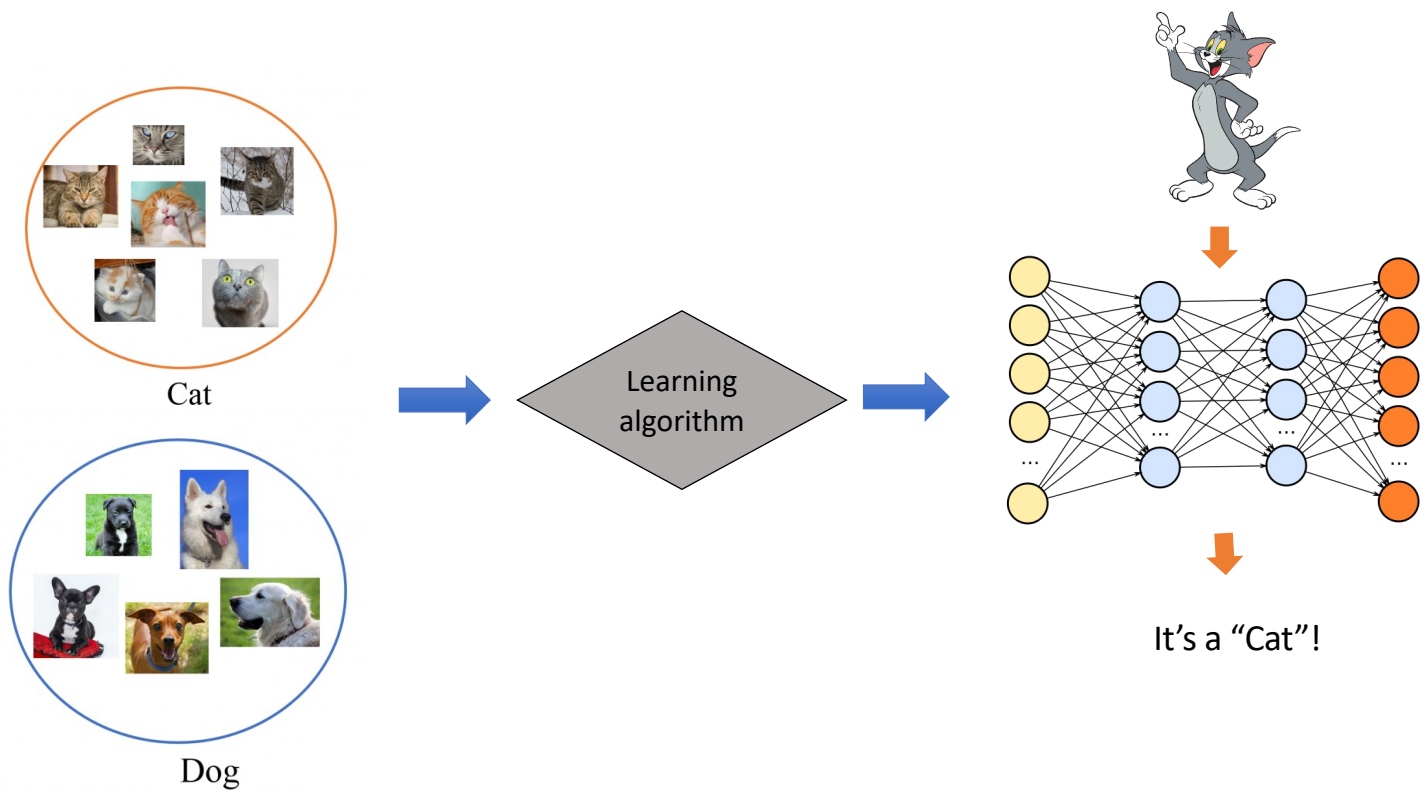
There will be some steep learning curves for some

- You need to use math:
 - Calculus, Linear Algebra, Probabilities.
 - Follow mathematical proofs.
- You need to be able to code:
 - Mainly in Python (numpy, scipy)
 - Learn to use pyTorch for coding assignments
- If you are/were a UCSB undergraduate:
 - This course overlaps with CS 165B but materials are covered with more breath and depth.
 - Having completed the following courses may help you: Linear algebra (MATH 3B), Vector Calculus (6A), Probability and Statistics (PSTAT 120A, 120B), data-structures and algorithms (CS 130A & 130B)

Remaining of today's lecture

- Machine learning overview
- Supervised learning by an example

Machine learning studies “*computer programs that automatically improve (its performance on a **task**) with **experience**.*”

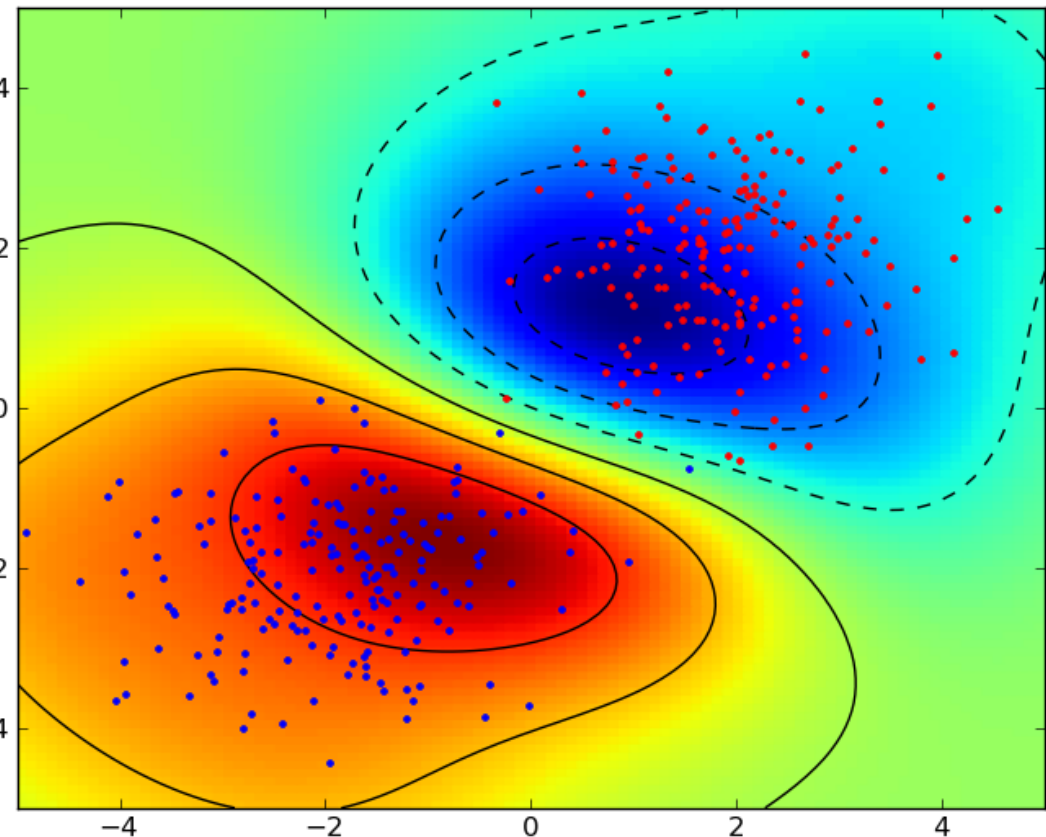
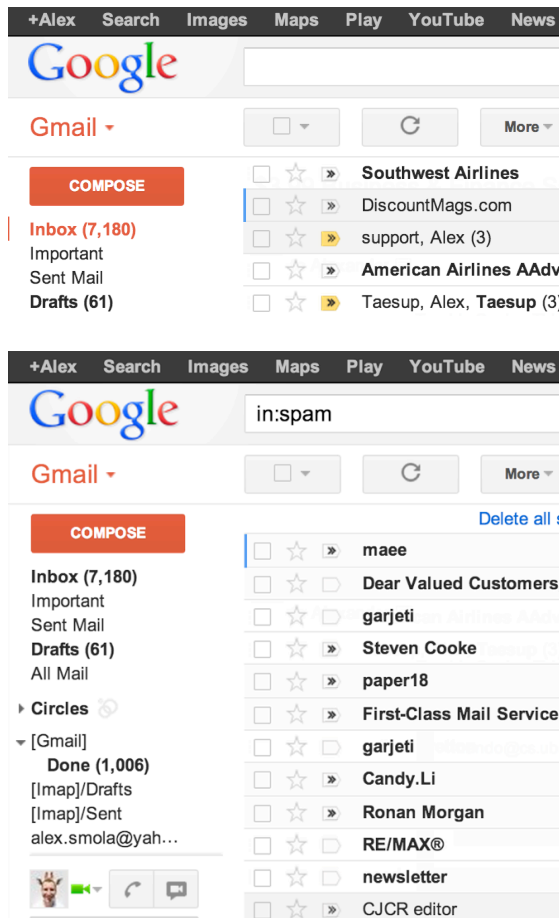


Different tasks / problems in Machine Learning

- Supervised Learning *Spam Filter.*
- Unsupervised Learning *Topics of a text corpus*
- Reinforcement Learning *Atari Games. Serve Ads.*
- Structured Prediction *Machine translation.*

Semi-supervised learning, active learning,
ranking /search / recommendation
self-supervised learning and many more!

Supervised learning is about predicting label y using feature x by learning from labeled examples.

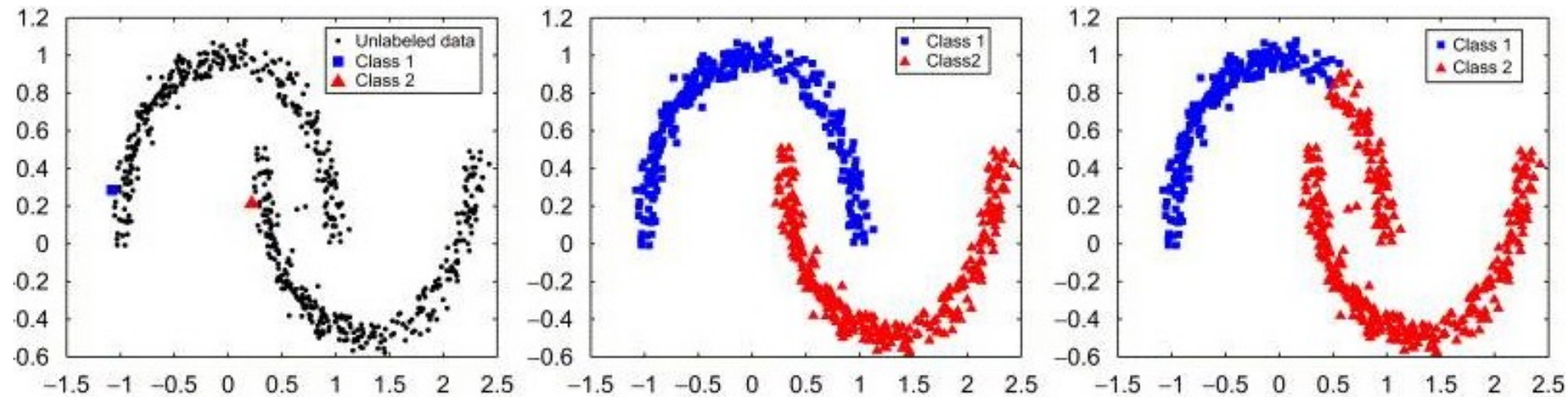


Unsupervised Learning is about finding structures in an unlabeled dataset

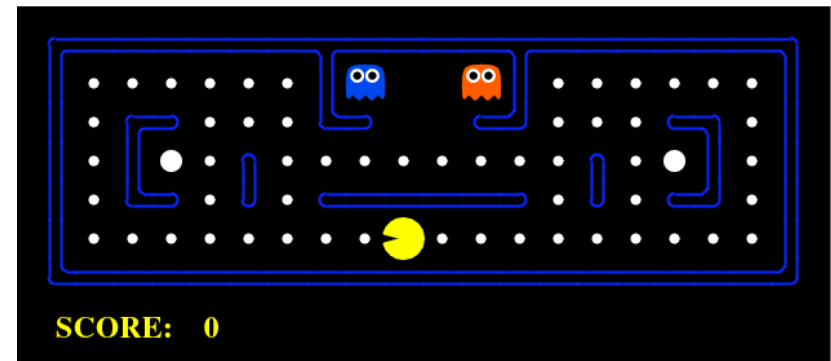
| “Arts” | “Budgets” | “Children” | “Education” |
|---------|------------|------------|-------------|
| NEW | MILLION | CHILDREN | SCHOOL |
| FILM | TAX | WOMEN | STUDENTS |
| SHOW | PROGRAM | PEOPLE | SCHOOLS |
| MUSIC | BUDGET | CHILD | EDUCATION |
| MOVIE | BILLION | YEARS | TEACHERS |
| PLAY | FEDERAL | FAMILIES | HIGH |
| MUSICAL | YEAR | WORK | PUBLIC |
| BEST | SPENDING | PARENTS | TEACHER |
| ACTOR | NEW | SAYS | BENNETT |
| FIRST | STATE | FAMILY | MANIGAT |
| YORK | PLAN | WELFARE | NAMPHY |
| OPERA | MONEY | MEN | STATE |
| THEATER | PROGRAMS | PERCENT | PRESIDENT |
| ACTRESS | GOVERNMENT | CARE | ELEMENTARY |
| LOVE | CONGRESS | LIFE | HAITI |

The William Randolph Hearst Foundation will give \$1.25 million to Lincoln Center, Metropolitan Opera Co., New York Philharmonic and Juilliard School. “Our board felt that we had a real opportunity to make a mark on the future of the performing arts with these grants an act every bit as important as our traditional areas of support in health, medical research, education and the social services,” Hearst Foundation President Randolph A. Hearst said Monday in announcing the grants. Lincoln Center’s share will be \$200,000 for its new building, which will house young artists and provide new public facilities. The Metropolitan Opera Co. and New York Philharmonic will receive \$400,000 each. The Juilliard School, where music and the performing arts are taught, will get \$250,000. The Hearst Foundation, a leading supporter of the Lincoln Center Consolidated Corporate Fund, will make its usual annual \$100,000 donation, too.

Semi-supervised Learning using both labeled and unlabeled data.



Reinforcement learning learns to make decisions for long-term rewards by trials-and-errors.



The Amazon logo, consisting of the word 'amazon' in a bold, black, lowercase sans-serif font with a curved orange arrow underneath it.

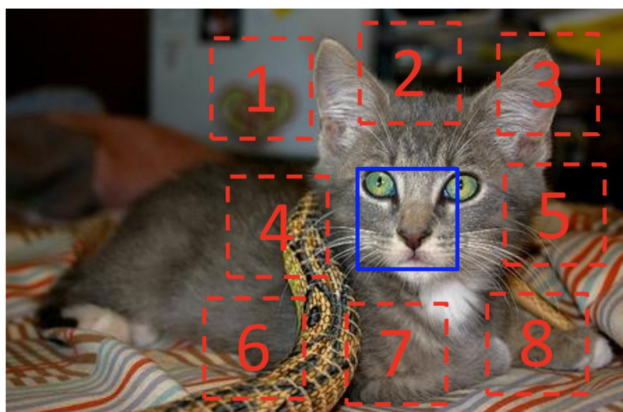
Recommendations



buy or not buy



Self-supervised learning learns to predict parts of x using other parts of x.



Example:



$$X = \left(\begin{array}{c} \text{[Kitten Face]} \\ \text{[Kitten Ear]} \end{array} \right); Y = 3$$

Question 1:



Question 2:



Randomly
masked

A quick [MASK] fox jumps over the [MASK] dog



Predict

A quick brown fox jumps over the lazy dog

Image example from [\(Doersch et al, 2015\)](#), text example from [Amit Chaudhary](#)

Task, Experience, Performance

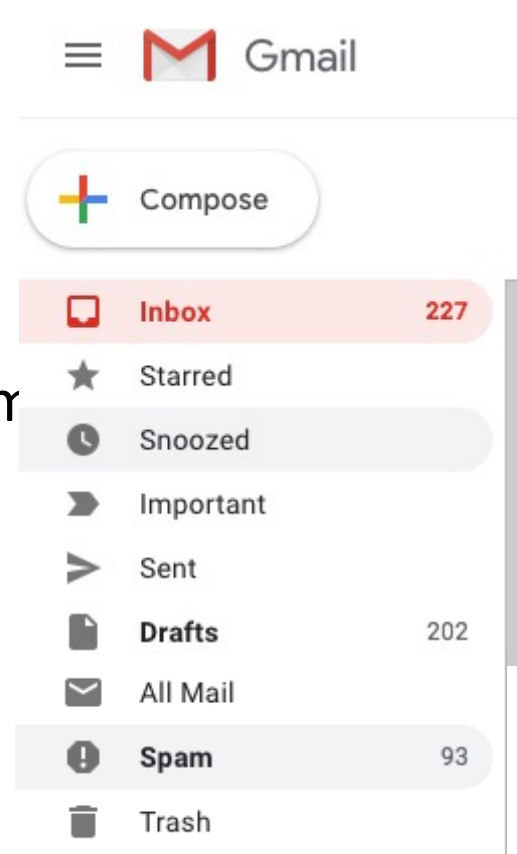
| | Task | Experience | Performance |
|--------------------------|--|--|---|
| Supervised learning | Use X predict Y | (X,Y) – feature-label pairs | error |
| Unsupervised learning | Organize, index, discover structures in data | Collection of unlabeled data X | “How well it represents actual data distribution” |
| Semi-supervised learning | Use X predict Y | Unlabeled data X, and labeled data (X,Y) | error |
| Reinforcement learning | Make savvy decisions | Feedback from Task environment | Expected Long-term reward |
| Self-supervised learning | Use one part of X to predict another part of X | Collection of unlabeled data X | Reconstruction error |

The focus of today's lecture is "Supervised Learning"

- Actually, just "binary classification".
- Prototypical Example: Spam filtering



Illustration extracted from [\[here\]](#)



Example of SPAM emails

Mail thinks this message is Junk Mail.

Move to Inbox

MICROWORLD CORPORATIO... December 20, 2019 at 2:38 AM

MC

CLAIMS.

To: undisclosed-recipients;;

Reply-To: microworld219@gmail.com

MICROWORLD CORPORATIONS:
CUSTOMER SERVICE:
FRIEDRICHSTRAË 10,BERLIN ALEMANHA
REFERENCE NUMBER: MBB-009-D54-DE
BATCH NUMBER: MGC-2019- SM-009
TICKET NUMBERS: 2,6,13,21,26,32

OFFICIAL WINNING NOTIFICATION.

We are pleased to inform you of the released results of Microworld Promotion... This is a promotional program organized by Microworld Corporations, in conjunction with the Foundation for the promotion of software products, and use of email addresses. Held on Thursday 19th, December 2019, in Berlin, Alemanha. Your email address won a cash award of Four hundred and eighty eight thousand two hundred and fifty euros (488,250.00 Euros).. Contact Our Foreign Transfer Manager for claims with your winning details and your contact information. Mrs. Helena Bosch.
Email: micropromo19@yahoo.com
Congratulations!!
Sincerely,
Rosa Van Beek.

Mail thinks this message is Junk Mail.

Move to Inbox

Email ADMIN

January 1, 2020 at 10:35 PM

EA

cs.ucsb.edu APPLICATION -Storage Full Notes- Last -... [Details](#)

To: Yu-Xiang Wang,

Reply-To: Email ADMIN

Dear yuxiangw@cs.ucsb.edu,

Your email has used up the storage limit of 99.9 gigabytes as defined by your Administrator. You will be blocked from sending and receiving messages if not re-validated within **48hrs**. Kindly click on your email below for quick re-validation and additional storage will be updated automatically

yuxiangw@cs.ucsb.edu

Regards,
E-mail Support 2020.

Example of another SPAM email

Mail thinks this message is Junk Mail.

Move to Inbox

☆ MARK ZUCKERBERG

Junk - Google August 24, 2018 at 10:48 AM

MZ

WINNING AMOUNT

Reply-To: MARK ZUCKERBERG

WINNING AMOUNT

My name is Mark Zuckerberg, A philanthropist the founder and CEO of the social-networking website Facebook, as well as one of the world's youngest billionaires and Chairman of the Mark Zuckerberg Charitable Foundation, One of the largest private foundations in the world. I believe strongly in 'giving while living' I had one idea that never changed in my mind - that you should use your wealth to help people and i have decided to secretly give {\$1,500,000.00} to randomly selected individuals worldwide. On receipt of this email, you should count yourself as the lucky individual. Your email address was chosen online while searching at random. Kindly get back to me at your earliest convenience, so I know your email address is valid. (mzuckerberg2444@gmail.com) Email me Visit the web page to know more about me: https://en.wikipedia.org/wiki/Mark_Zuckerberg/ or you can google me (Mark Zuckerberg)

Regards,
MARK ZUCKERBERG

Example of a HAM (non-spam) email



Dear Professor Foo,

I am a student in your machine learning class.

I have a question about the second term project and I was not able to find the answer on the syllabus. Should our project be only about the topics listed on the second part of the syllabus, or can I incorporate topics from the whole course, as long as it fits with the subject of the class?

I look forward to hearing from you.

Best regards,

Bar

Quoted from [[Here](#)].

Modeling-Inference-Learning

Modeling

- Feature engineering
- Specify a family of classifiers

Inference

Apply the classifier to emails

Learning

Learning the best performing classifier

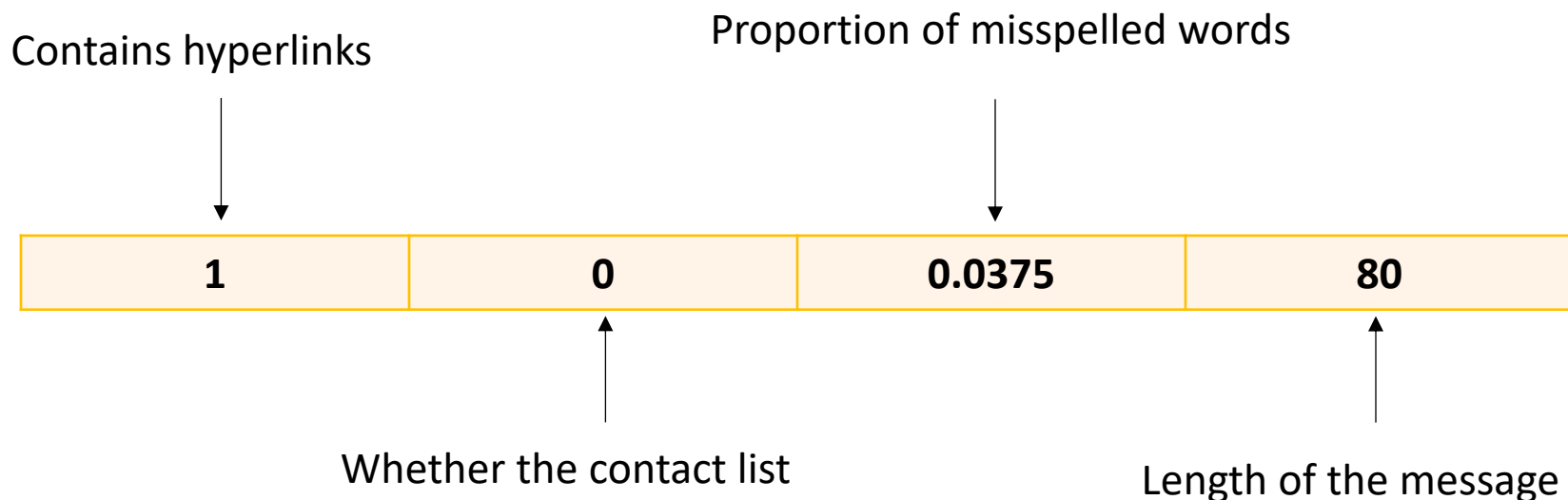
What are the features that we can use to describe an email (3 min discussion)

- What are the information that we can extract from text, and hyper-texts to describe an email?
- What are typical characteristics of a spam email?
- What are typical characteristics of a non-spam email?

Possible features

- Number of special characters: \$, %
 - Mentioning of: Award, cash, free
 - Greetings: generic, or specific
 - Bad grammars and misspelled words: e.g. m0ney, c1ick here.
 - Excessive excitement: Many “!”, “!!!”, “?!”, words in CAPITAL LETTERS.
-
- Whether the senders on the contact list
 - Length of an email
 - Whether the receiver has responded to sender before

Example of a feature vector of dimension 4



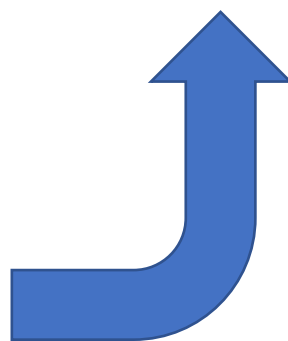
Email ADMIN January 1, 2020 at 10:35 PM EA
[\(cs.ucsb.edu\)](#) APPLICATION -Storage Full Notes- Last -... Details
To: Yu-Xiang Wang,
Reply-To: Email ADMIN

Dear yuxiangw@cs.ucsb.edu,

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yuxiangw@cs.ucsb.edu

Regards,
E-mail Support 2020.

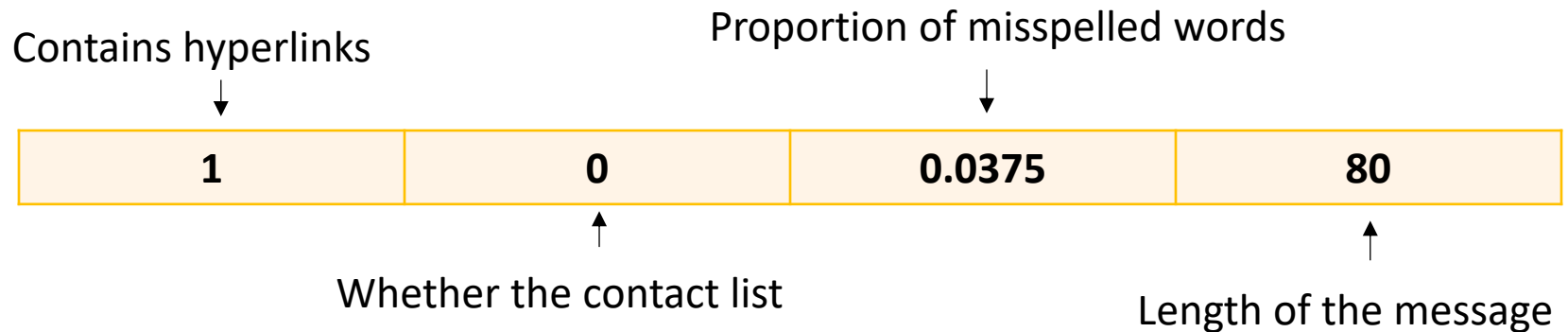


**Step 1 in Modelling
Feature extractor:**
Converting the object of interest
to a vector of numerical values.

Mathematically defining a classifier

- Feature space: $\mathcal{X} = \mathbb{R}^d$
- Label space: $\mathcal{Y} = \{0, 1\} = \{\text{non-spam}, \text{spam}\}$
- A classifier (hypothesis): $h : \mathcal{X} \rightarrow \mathcal{Y}$

How do we make use of this feature vector? What is a reasonable “classifier” based on this feature representation?



- Feature space: $\{0, 1\} \times \{0, 1\} \times \mathbb{R} \times \mathbb{N}$
- Label space: $\mathcal{Y} = \{0, 1\} = \{\text{non-spam}, \text{spam}\}$
- **How are we going to use these features as a human?**
 - (3 min discussion)

Specifying a family of classifiers -- - a “hypothesis class”

- Hypothesis class
 - A family of classifiers: \mathcal{H}
 - Also known as “concept classes”, “models”, “decision rule book”
 - “Neural networks” and “Support Vector Machines” are hypothesis classes.
 - Typically we want this family to be large and flexible.

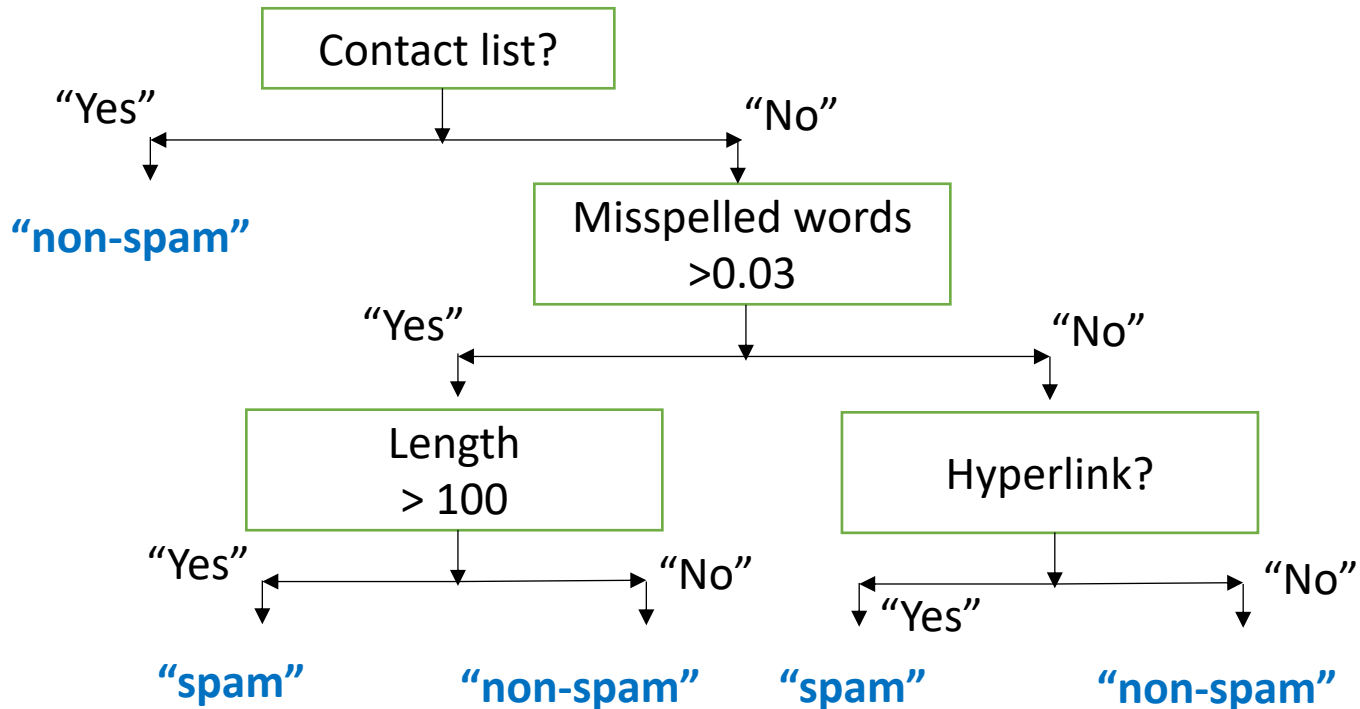
- The task of machine learning:

- A **selection problem** to find a

$$h \in \mathcal{H}$$

that “**works well**” on this problem using the **observed data**.

Decision trees



- **Question:** What are the “free parameters” if we are to learn such a decision tree? Using data?

Learning a decision tree

- Free parameters:
 - Which feature(s) to use when branching branch?
 - How to branch? Thresholding? Free threshold?
 - Which label to assign at leaf nodes?
- Hyperparameters:
 - Max height of a decision tree?
 - Number of parameters the tree can use in each
- **Question:** Consider a problem with **4 binary features**.
 - How many decision trees of **3 layers** are there? If each decision uses only one feature? (you may repeat features)
 - How many possible feature vectors are there?
 - How many classifiers are there (without restrictions)?

Example: Linear classifiers

- $\text{Score}(x) = w_0 + w_1 * \mathbf{1}(\text{hyperlinks}) + w_2 * \mathbf{1}(\text{contact list}) + w_3 * \text{misspelling} + w_4 * \text{length}$
- A linear classifier: $h(x) = 1$ if $\text{Score}(x) > 0$ and 0 otherwise.
- Question: What are the “free-parameters” in a linear classifier?

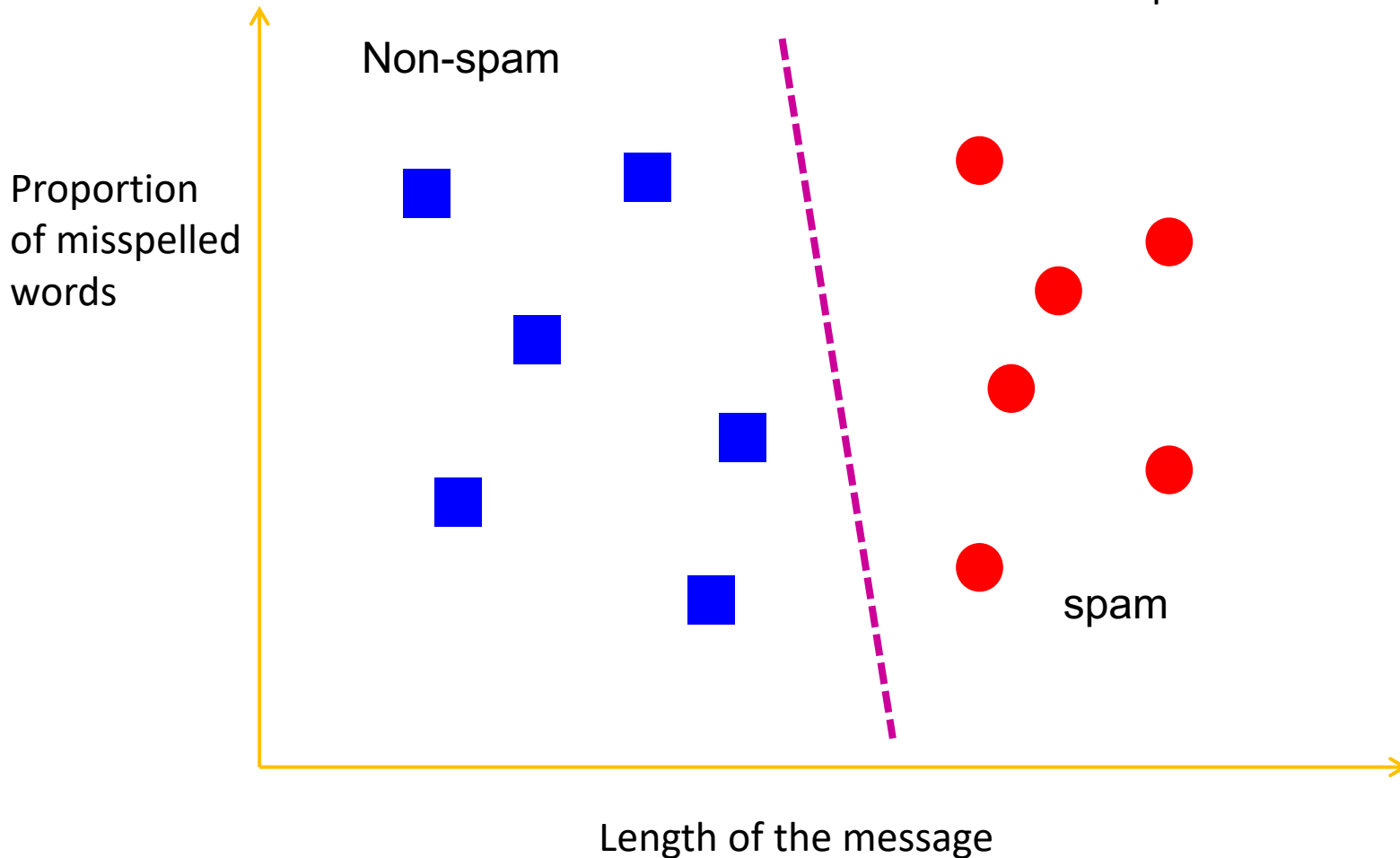
- If we redefine $\mathcal{Y} = \{-1, 1\}$

- A compact representation:

$$h(x) = \text{sign}(w^T [1; x])$$

Geometric view: Linear classifier are “half-spaces”!

$\{x \mid w_0 + w_1 * x_1 + w_2 * x_2 + w_3 * x_3 + w_4 * x_4 > 0\}$
The set of all “emails” that will be classified as “Spams”.



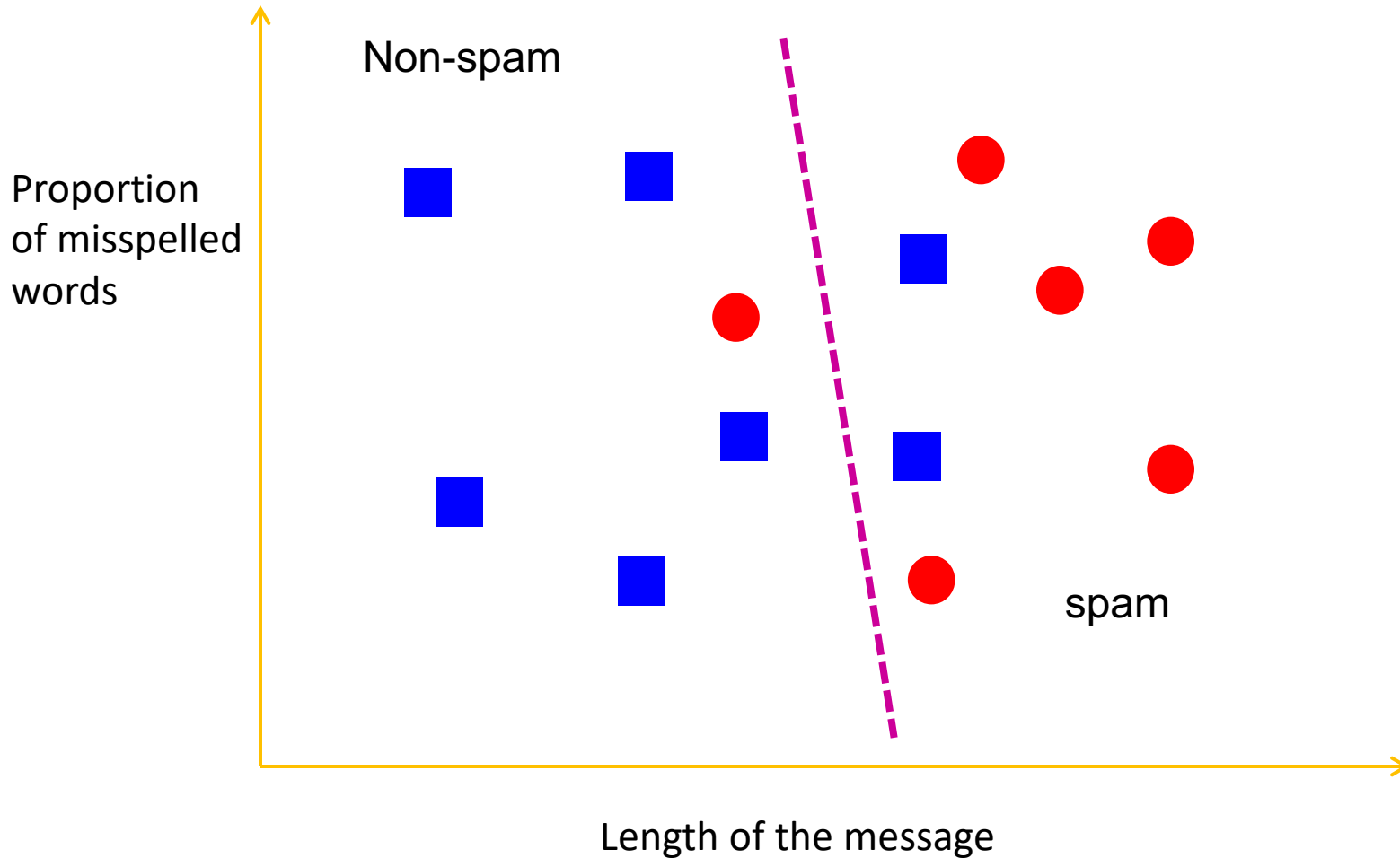
Learning linear classifiers

- Training data:

$$(x_1, y_1), \dots, (x_n, y_n) \in \mathcal{X} \times \mathcal{Y}$$

- In the above example, there is a clean cut boundary that distinguishes “spams” from “non-spams”.
 - “Linearly separable” problem
 - Learning linear classifier: Finding vector w that is consistent with the observed training data.

Example: Linearly non-separable cases



How do we learn a linear classifier in a non-linearly separable case?

- Training data:

$$(x_1, y_1), \dots, (x_n, y_n) \in \mathcal{X} \times \mathcal{Y}$$

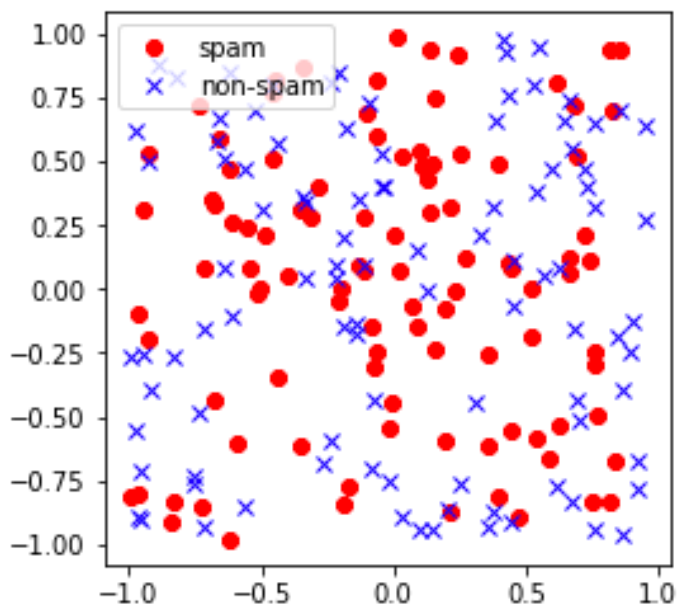
- Solving the following optimization problem:

$$\min_{w \in \mathbb{R}^d} \text{Error}(w) = \frac{1}{n} \sum_{i=1}^n \mathbf{1}(h_w(x_i) \neq y_i)$$

- Learning: Find the linear classifier that makes **the smallest number of mistakes** on the training data.

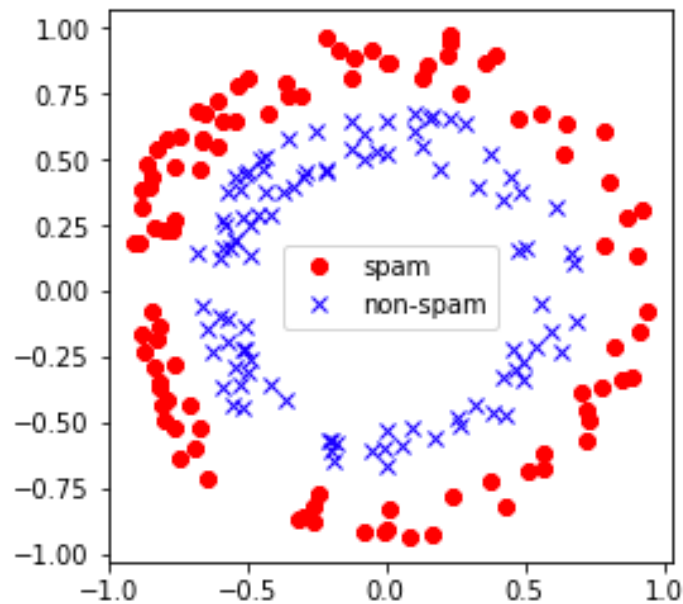
What happens if the linear classifier with the smallest number of mistakes still makes a mistake 49% of the time?

Case 1:



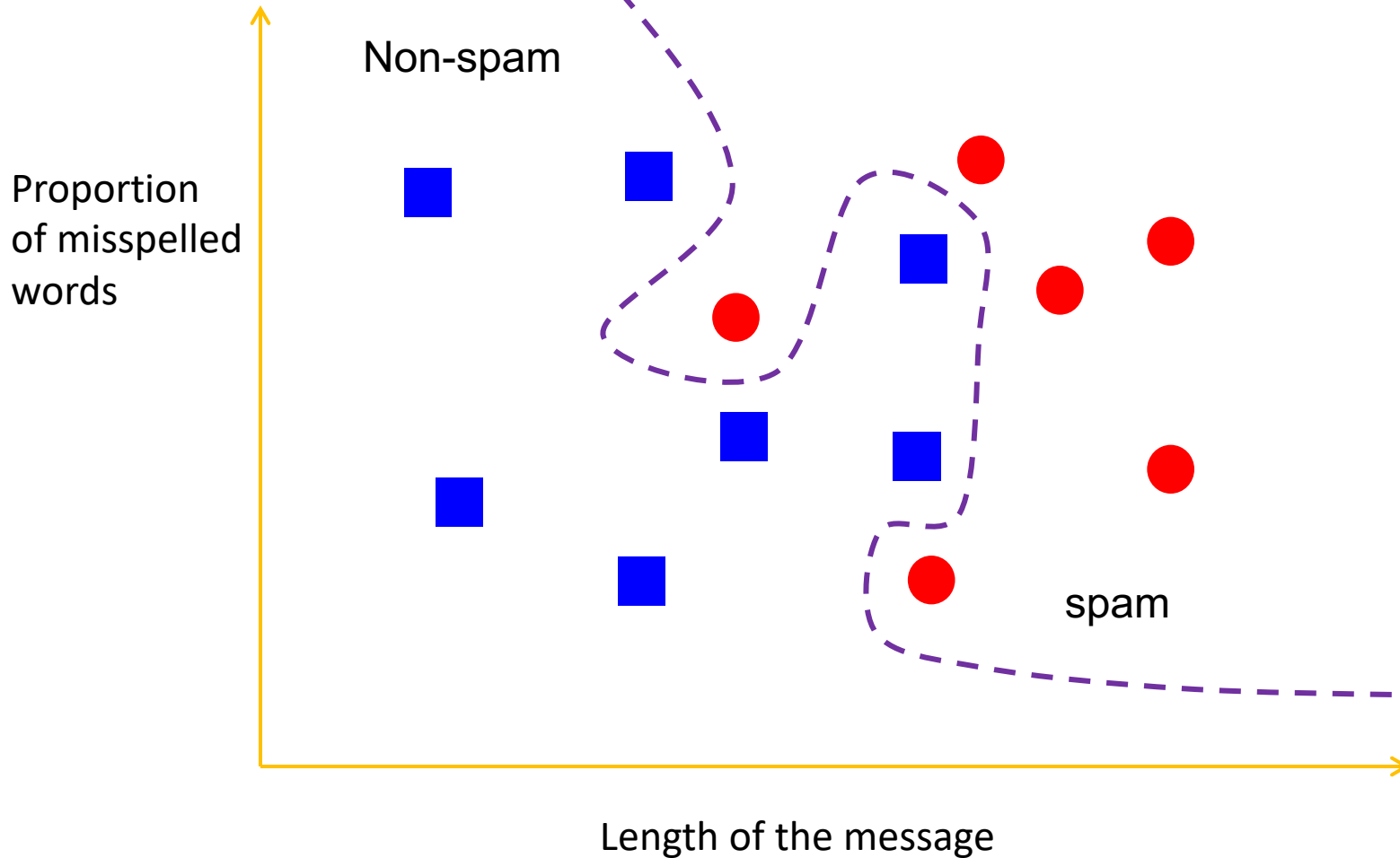
There is no information about the label in the features.
No classifiers are able to do well.

Case 2:

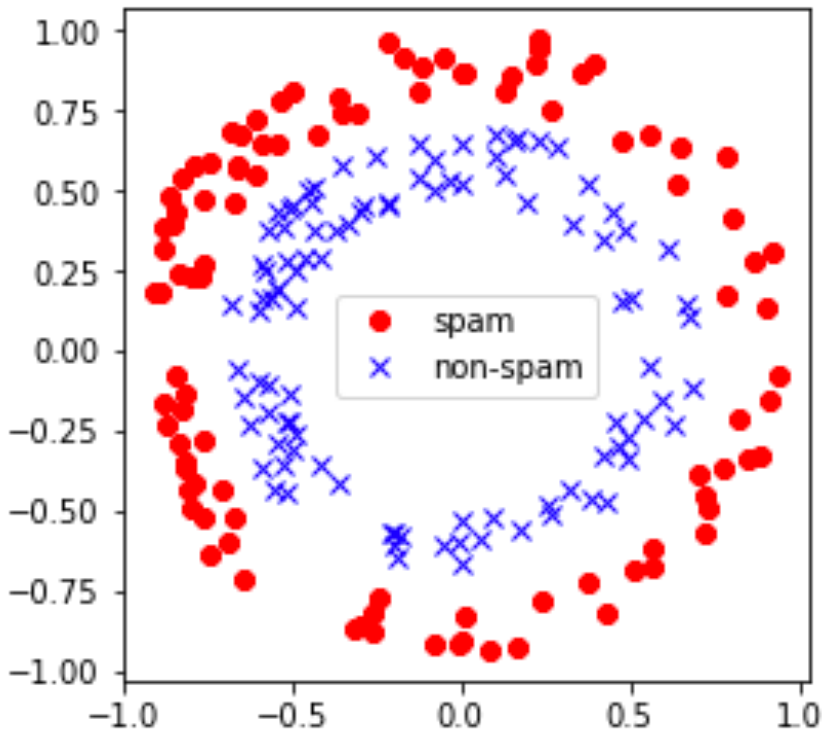


There are some nonlinear classifier that works. But no linear classifiers will do better than chance.

Going to higher dimensions? Maybe we can also allow non-linear decision boundaries?



Example: Feature transformation.



What we can do:

$$(\tilde{x}_1, \tilde{x}_2) = \left(\sqrt{x_1^2 + x_2^2}, \arctan(x_2/x_1) \right)$$

In the redefined space, the two classes are now linearly separable.

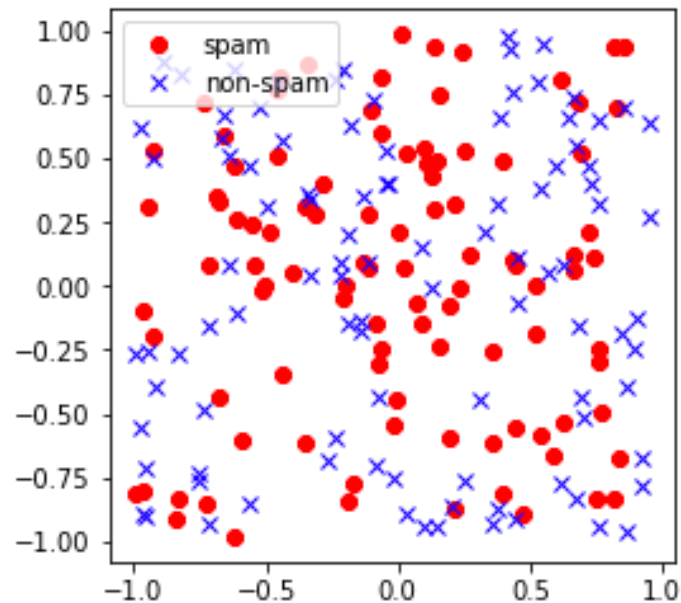
Nonparametric classifiers

- Increasing the complexity of the classifier as we get more data
- For example:
 - We can use the entire training dataset as “free parameters” of the classifier.
 - k-Nearest Neighbor
 - Kernel methods (lifting to infinite dimensional space)
 - Neural networks (design a model for a fixed data size)

Question: What is the classification error of 1-NN classifiers?

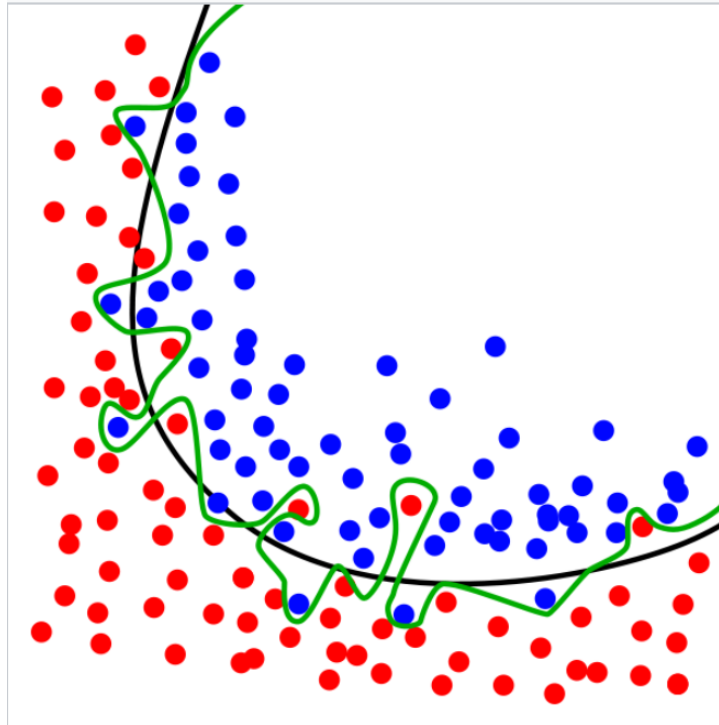
We can make the classifiers arbitrarily accurate... with 1-NN classifier; or with bigger and bigger neural networks.

- Even if the data look like:



- **What went wrong?**

The problem of Overfitting



The green line represents an overfitted model. While the green line best follows the training data, it is too dependent on that data and it is likely to have a higher error rate on new unseen data.

The goal of machine learning is not to obtain 0-training error, but rather to achieve small error rates on **new data points** (that are **not** used for training.)

- Test Error < Training Error + Generalization Error

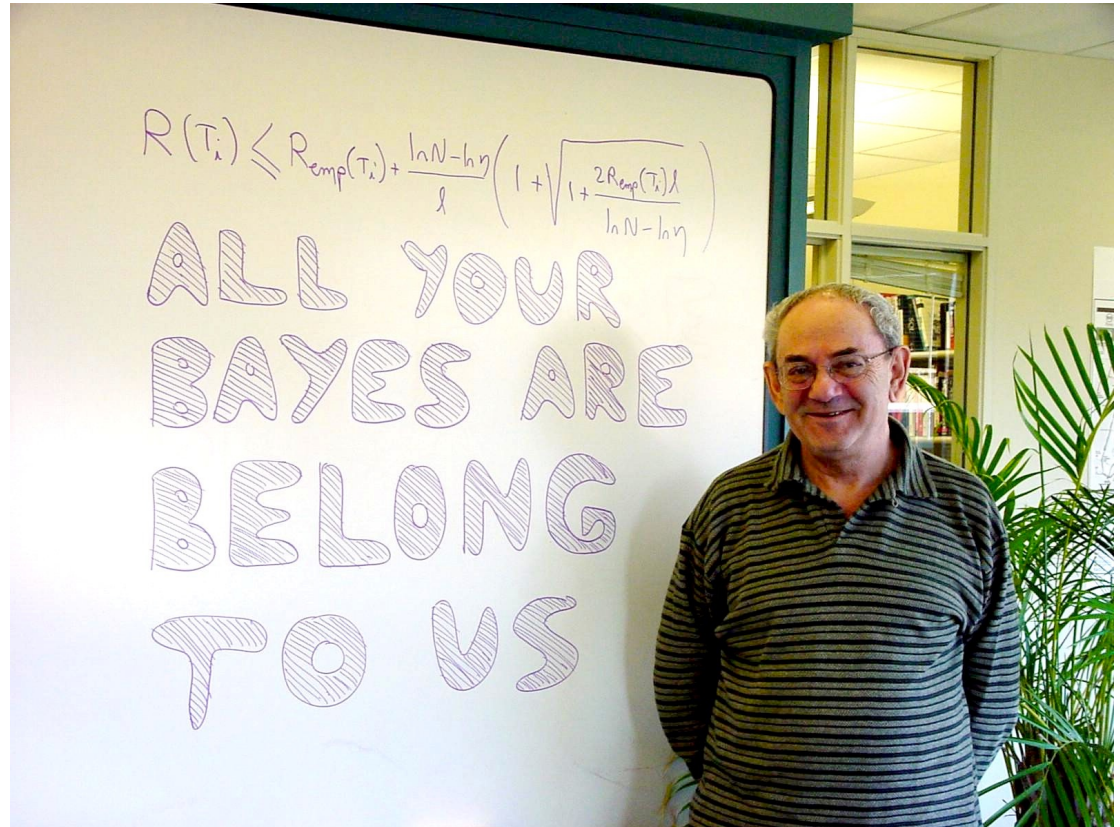
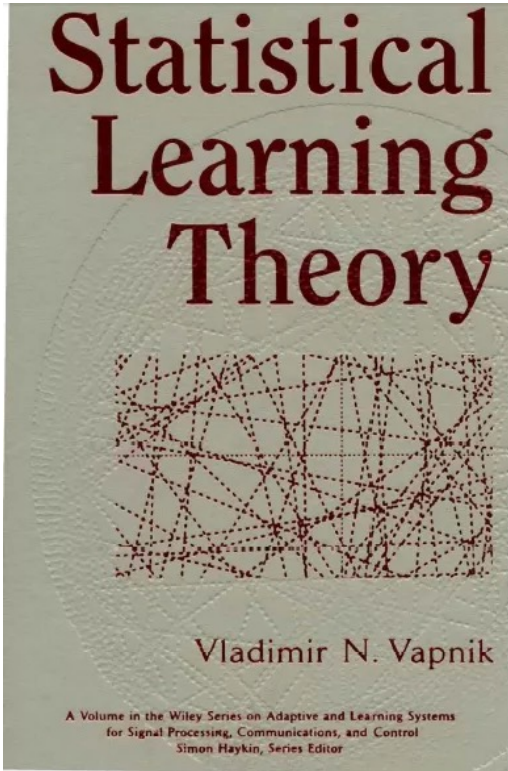
$$\text{Err}(h) := \mathbb{E}[\mathbf{1}(h(x) \neq y)] \quad \widehat{\text{Err}}(h) := \frac{1}{n} \sum_{i=1}^n \mathbf{1}(h(x_i) \neq y_i)$$

$$\text{Gen}(\mathcal{H}) := \sup_{h \in \mathcal{H}} \left| \frac{1}{n} \sum_{i=1}^n \mathbf{1}(h(x_i) \neq y_i) - \mathbb{E}[\mathbf{1}(h(x) \neq y)] \right|$$

(** some text uses “generalization error” as a synonym as “test error”, which has created much confusion. The above is the definition we adopt.)

Statistical Learning Theory

TL;DR: Proving that the generalization error $\rightarrow 0$, thus showing that ML works.



Closely related to Empirical Process Theory, Computational Learning Theory.

Summary of today's lecture

- Machine learning overview
- Supervised learning: Spam filtering as an example
 - Features, feature extraction
 - Models, hypothesis class
 - Choosing an appropriate hypothesis class
 - Performance metric
 - Overfitting and generalization

Next lecture: more on supervised learning

- Supervised learning: problem setup
- Loss function, Risk, Empirical Risk
 - Risk decomposition
 - Analysis of linear regression under linear gaussian model
 - Analysis of supervised learning with bounded loss
- Model-selection: Holdout, Cross-validation